Minimization of FSA

Data Structures and Algorithms for Comp (ISCL-BA-07) nal Linguistics III

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Finding equivalent states



Their right languages are the same

Minimization by partitioning



- Accepting & non-accept partition
- For any of the nodes in a set, if any symbol leads to different sets of nodes, split
- $Q_1 = \{0,3\}, Q_2 = \{1\}, Q_2 = \{2\}, Q_2 = \{2\}, Q_3 = \{2\}, Q_4 =$
- Stop when we cannot split any of the sets, merge the indistinguishable states

DFA minimization

- By finding the minimal DFA, we can also prove equivalence (or not) of different FSA and the languages they recognize
- In general the idea is:
- * For any regular language, there is a unique minimal DFA
- in goatest acter acted to conclude attack (easy)
 Merge equipulent states
 There are two well-known algorithms for minimization:
 There are two well-known algorithms for minimization:
 Hopcreft's algorithms find and eliminate equivalent states by partitioning the set of states
 Bizzazzowski's algorithms: 'devolbe reversal'

Finding equivalent states



The edges leaving the group of nodes are identical Their right languages are the same.

Minimization by partitioning



* Create a state-by-state table, mark distinguishable pairs: (q_1,q_2) such that $(\Delta(q_1,x),\Delta(q_2,x))$ is a distinguishable pair for any $x\in \Sigma$



Minimization by partitioning



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Minimization by partitioning



Create a state-by-state table, mark distinguishable pairs: (q_1, q_2) such that $(\Delta(q_1, x), \Delta(q_2, x))$ is a distinguishable pair for any $x \in \Sigma$



Minimization by partitioning





Minimization by partitioning

Create a state-by-state table, mark distinguishable pairs: (q₁, q₂) such that (Δ(q₁, x), Δ(q₂, x)) is a distinguishable pair for any x ∈ Σ



Minimization by partitioning



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Minimization by partitioning

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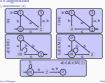


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- The algorithm can be cell to visit carefully

Brzozowski's algorithm



Minimization algorithms

An exercise



• FST

There are many versions of the 'partitioning' algorithm. General idea is to form equivalence classes based on right-language of each state.

Partitioning algorithm has O(n log n) complexity 'Double reversal' algorithm has exponential worst-time complexity

 Double reversal algorithm can also be used with NFAs (resulting in the minimal equivalent DFA – NFA minimization is intractable) ner, different alg

different input Reading suggesti ion: Hopcroft and Ullman (1979, Ch. 2&3), Jurafsky and Martin (2009, Ch. 2)

FSA and regular language

Acknowledgments, credits, references

Hopcroft, John E. and Jeffrey D. Ullman (1979). Introduction to Automata Theory, Languages, and Computation. Addison-Wesley Series in Computer Science and

Languages, and Computation. Addison-Wesley Series in Computer Science and Information Processing. Addison-Wesley. user 9902011205889. Jurafsky, Daniel and James H. Martin (2009). Speech and Language Processing: As Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition. second edition. Pearson Prentice Hall. user: 978-013-304198-3.

