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Transforming one string to another

- The table (back arrows) also gives a set of edit operations to tra string to another
- For LCS, operations are
 - copy (diagonal arrows in the den
- insert (left arrows in the demo assuming original string is the vertical one)
 delete (up arrows in the demo) These also form an alignment between two strings
- · Different set of edit operations recovered will yield the same LCS, but different alignments

LCS alignments

| | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | |
|---|---|---|----|----|---|----|----|---|---|---|----------|
| | | ¢ | h | 1 | у | 8 | e | i | n | e | |
| 0 | c | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | A |
| 1 | h | 0 | 1+ | -1 | 1 | 1 | 1 | 1 | 1 | 1 | <u> </u> |
| 2 | y | 0 | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | с Ъ |
| 3 | g | 0 | 1 | 1 | 2 | 3. | -3 | 3 | 3 | 3 | - |
| 4 | 1 | 0 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 4 | c |
| 5 | c | 0 | 1 | 2 | 2 | 3 | 4+ | 4 | 4 | 5 | <u> </u> |
| 6 | n | 0 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 | |
| 7 | с | 0 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 6 | |

LCS - some remarks

- + We formulated the algorithm as maximizing the LCS
- + Alternatively, we can minimize the costs associated with each operation: - copy = 0 - delete = - insert =
- + The cost settings above are the typical, e.g., as in diff
- In some applications we may want to have different costs for delete and ins (e.g., mapping lemmas to inflected forms of words)
- Similarly, we may want to assign different costs for differ higher cost to delete consonants in historical linguistics) nt characters (e.g.



Edit distance: extensions and variations

- · Another possible operation we did not cover is some (or transpose), which is useful for applications like spell checking
- + In some applications (e.g., machine translation, OCR correction) we may
- want to have one-to-many or many-to-one alignments
- Additional requirements often introduce additional complexity
- · It is sometimes useful to learn costs from data

Acknowledgments, credits, references

- Goodrich, Michael T., Roberto Tamassia, and Michael H. Goldwasser (2013). Data Structures and Algorithms in Python. John Wiley & Sons, Incorporated. so
- Data Structures and acquirement of generative systems of the system o

if len(Yy) = 0

if len(Xx) = 0

if x = y

-eine

Levenshtein distance

- · Levenshtein difference between two strings is the total cost of inserti deletions and substitut
- · With cost of 1 for all operations

 $\int len(X)$ len(Y) $lev(Xx,Yy) = \begin{cases} lev(X,Y) \end{cases}$ $1 + \min \begin{cases} lev(X, Yy) \\ lev(Xx, Y) \\ lev(X, Y) \end{cases}$

· Naive recursion (as defined above), again, is intractable

+ But, the same dynamic programming method works



| | | c | h | 1 | у | 8 | е | 1 | n | e |
|-----|---|---|----|----|---|----|-----|-----|---|---|
| 0 | c | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 1 | h | 1 | 0+ | -1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 2 | y | 2 | 1 | 1 | 1 | 2 | 3 | 4 | 5 | 6 |
| 3 | 8 | 3 | 2 | 2 | 2 | 1. | -2 | 3 | 4 | 5 |
| 4 | 1 | 4 | 3 | 2 | 3 | 2 | 2 | 2 | 3 | 4 |
| 5 | с | 5 | 4 | 3 | 3 | 3 | 2 + | N., | 3 | 3 |
| 6 | n | 6 | 5 | 4 | 4 | 4 | 3 | 3 | 3 | 4 |
| 7 | с | 7 | 6 | 5 | 5 | 5 | 4 | 4 | 4 | 3 |
| - 1 | | | - | | | | | | | |

Summary

- + Edit distance is an important problem in many fields including computational linguistics
- A number of related problems can be efficiently solved by dyn
- programming Edit distance is also important for approximate string matching and alignm
- Reading suggestion: Goodrich, Tamassia, and Goldwasser (2013, chapter 13), Jurašsky and Martin (2009, section 3.11, or 2.5 in online draft)
- Next

· Algorithms on strings: tries

· Reading: Goodrich, Tamassia, and Goldwasser (2013, chapter 13),

